

Cold atoms

1: Bose-Einstein Condensation

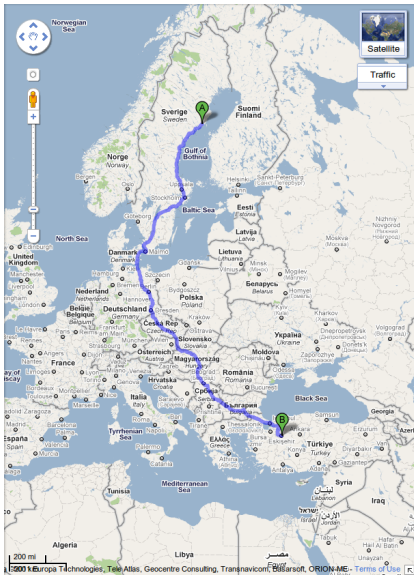
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Umeå



114 000 inhabitants
 Average age 37.9 years
 Cultural capital of Europe 2014
 400 km ski tracks
 180 km bicycle paths
 Umeå University with 35 435 students



Master programmes in:

- Computational Physics
- Condensed Matter Physics/Nanotechnology
- Theoretical Physics
- Optical Physics/Measurement Physics
- Quantum Mechanics/Quantum Technique
- Space Physics

Lectures

- 1: Bose-Einstein Condensation (today)
- 2: Quantum Hydrodynamics
- 3: Optical lattices

Cold atoms: a hot topic

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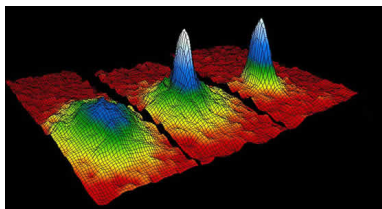
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- Detection: Photo of actual density!



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Energy of a matter wave is related to wavelength

$$E \sim \frac{\hbar^2}{m\lambda^2}$$

Long wavelengths means low energies – low temperatures!

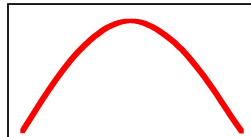
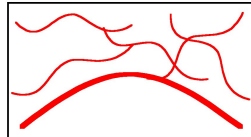
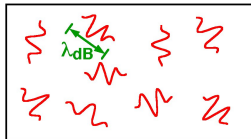
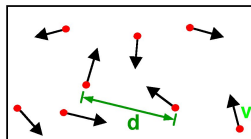
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- $3N$ -dimensional space: the problem scales exponentially with number of particles. (L^{3N})
- Historically: Solid materials, nuclei, or liquid helium. Now have quantum *gases* - more versatile

(blackboard lecture)

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- 2007: BEC in polaritons in semiconductors (Snoke)

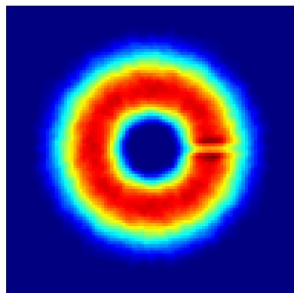
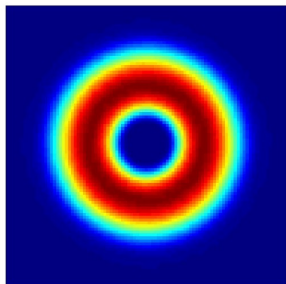
Gross-Pitaevskii equation

$$i\hbar \frac{\partial \Psi}{\partial t} = -\frac{\hbar^2}{2m} \nabla^2 \Psi + V(r)\Psi + U_0 |\Psi|^2 \Psi$$

GPE is used to simulate: ...

Gross-Pitaevskii equation

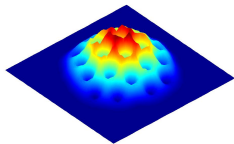
Ground state in various traps ...



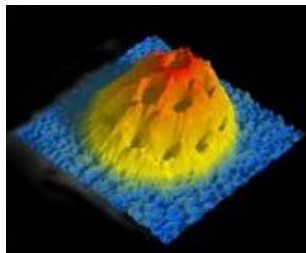
(BEC in a toroidal trap; work in progress)

Gross-Pitaevskii equation

... vortex lattices in rotated BECs ...



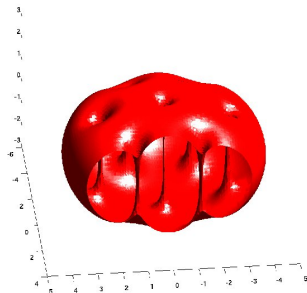
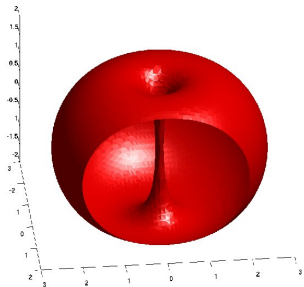
Theory



Experiment

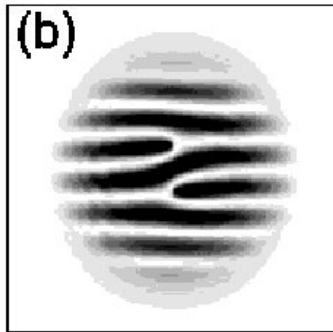
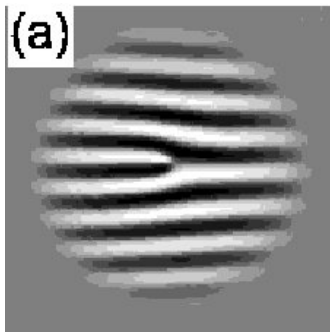
Gross-Pitaevskii equation

... More vortices (now in 3D) ...



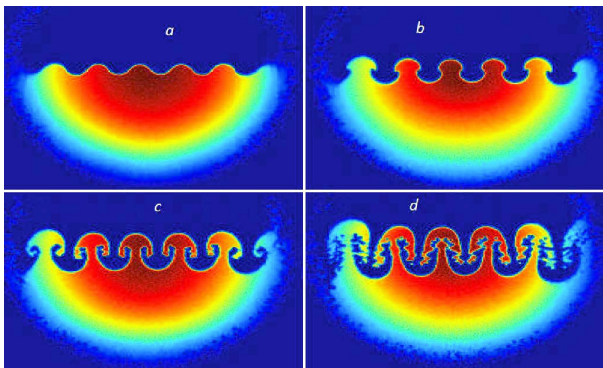
Gross-Pitaevskii equation

... coherence, correlations, interference fringes ...



Gross-Pitaevskii equation

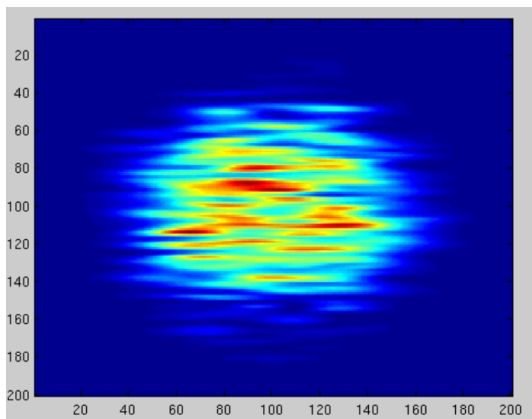
... systems of several condensates ...



Rayleigh-Taylor instability in an interface between two condensates
(More about this in Lecture 3)

Gross-Pitaevskii equation

...even finite-temperature physics and critical phenomena
(with modifications)



End of lecture 1

Thank you for your attention