

# Networks of Scientific Collaborations and Citations

---

Petter Holme

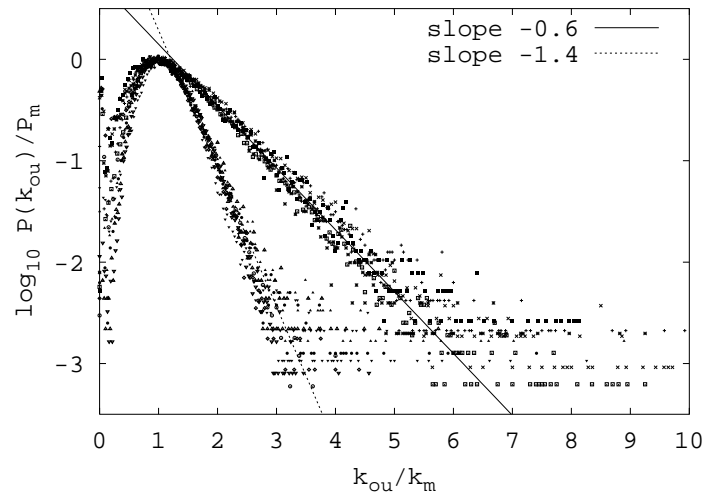
11th May 2001

## References:

- [1.] M. E. J. Newman, *Who is the best connected scientist? A study of scientific coauthorship networks*, cond-mat/0011144.
- [2.] A. L. Barabási *et al.*, *Evolution of the network of scientific collaborations*, cond-mat/0104162.
- [3.] A. Vazquez, *Statistics of citation networks*, cond-mat/0105031.
- [4.] A. Vazquez, *Knowing a network by walking on it: Emergence of Scaling*, cond-mat/0006132.

# CITATION NETWORKS

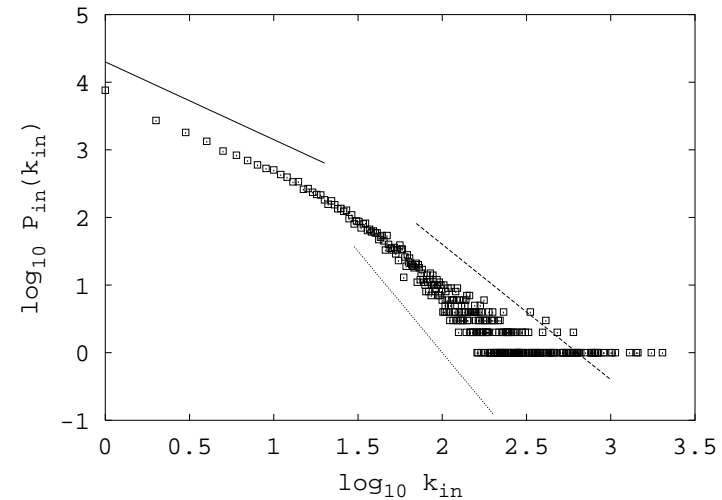
## Out Degree



The connectivity distribution of one paper's citations to other papers.

Large  $k$  power-law with non-integer exponent.

## In Degree

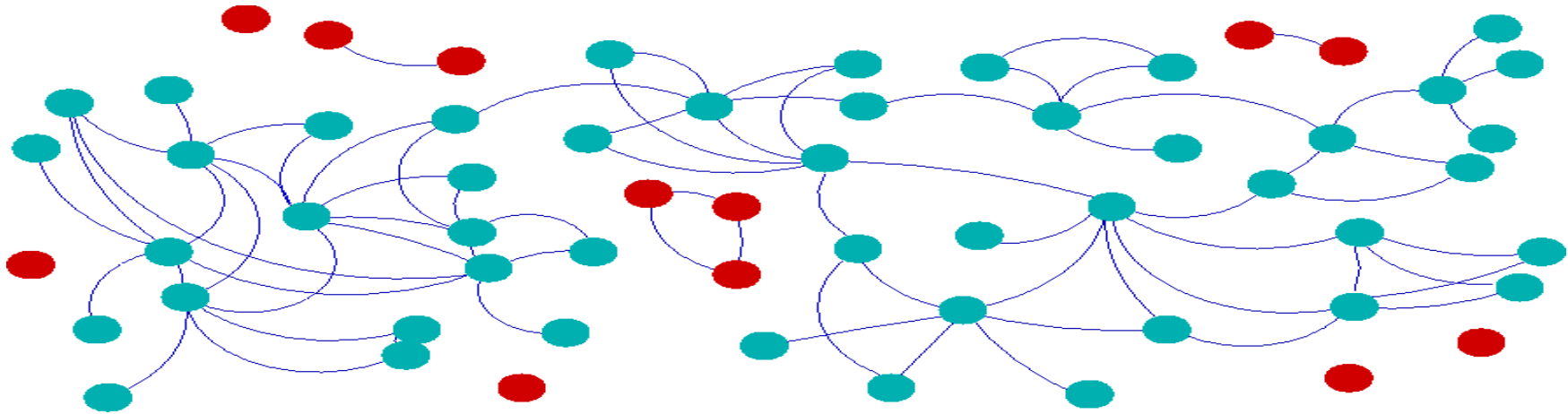


The connectivity distribution of citations from other papers to a specific paper.

A slope 2  $\rightarrow$  slope 3 power-law.

# FACT AND FICTION ABOUT THE GIANT COMPONENT

---



Random graph theory (ER graphs and percolation on connected graphs):

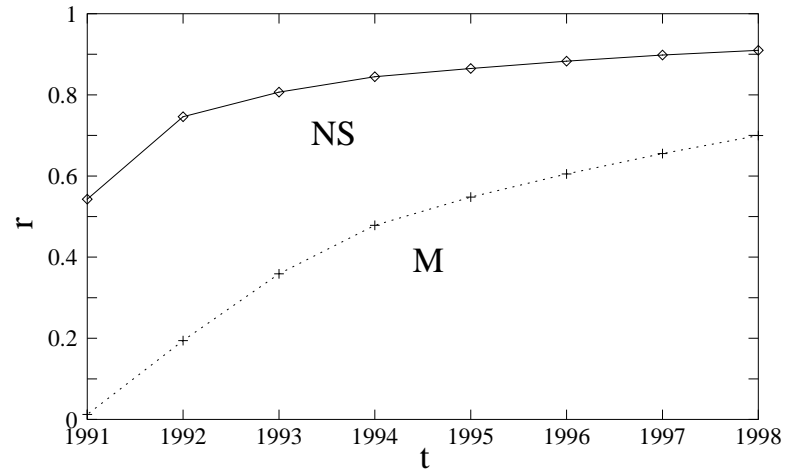
- Random graph theory: There is 2<sup>o</sup>-phase transition (for increasing number of edges) to a state with an extensively growing largest cluster, a **giant component**.

Real networks:

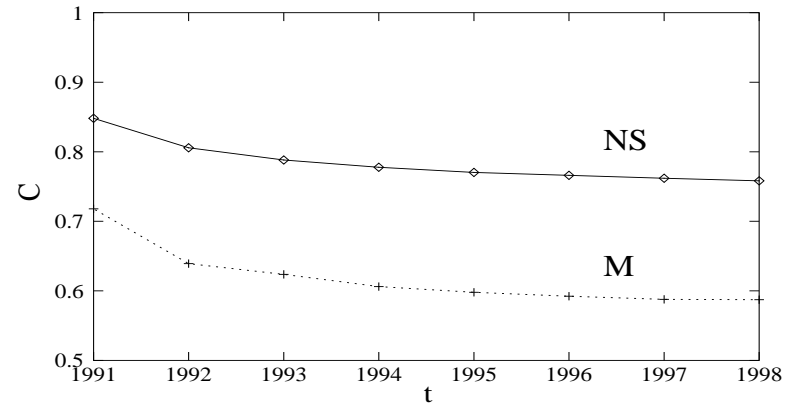
- Are disconnected.
- A vast majority belongs to one connected giant component.
- Characteristic lengths and clustering coefficients are calculated within the giant component.

# EVOLVING OF SCIENTIFIC COLLABORATIONS

## Giant Component



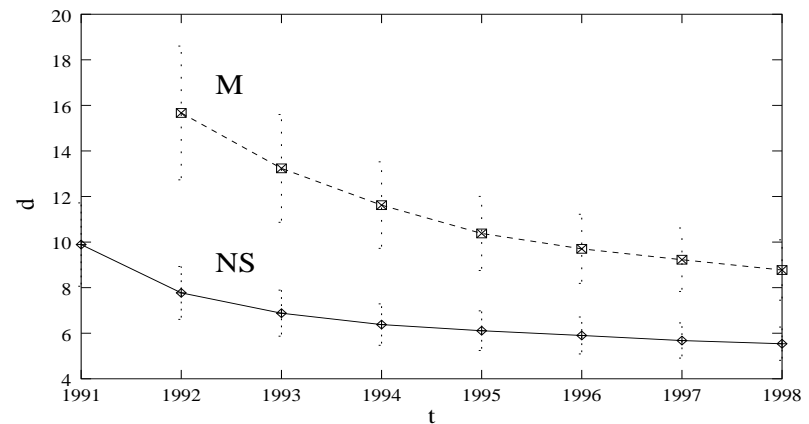
## Clustering Coefficient



Cumulative data up to indicated year.

- Large  $k$  power-law tail with slope  $\sim 2$ .
- Increasing average connectivity.

## Average Shortest Distance



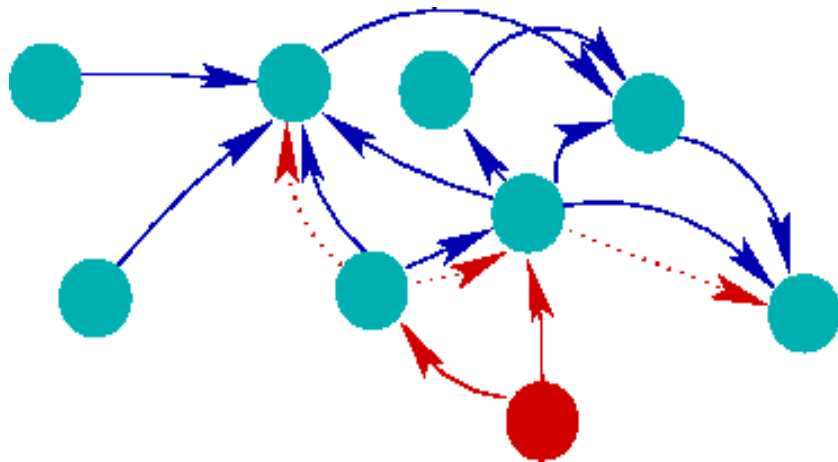
# NEW SCALE FREE NETWORK MODELS

---

## Recursive Search Model

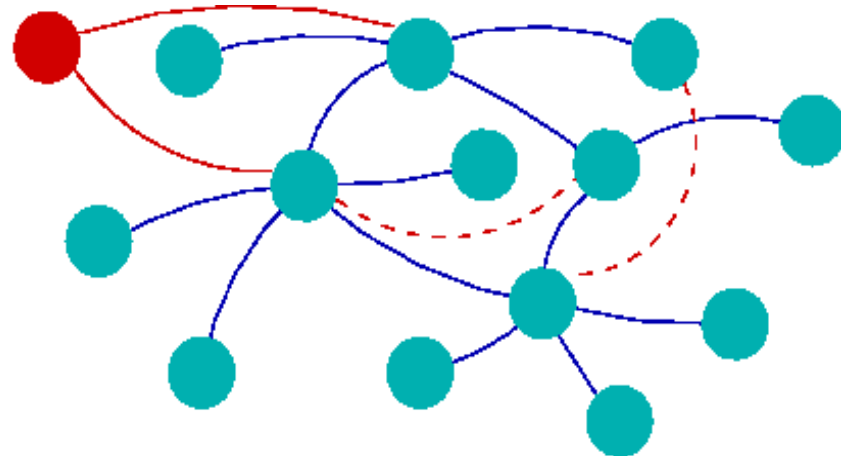
Directed graph.

- *Initial condition.* One node, no links.
- *Adding rule.* Add one node, and a link to another (randomly selected).
- *Walking rule.* The new node “walks” through the nodes pointed to by the selected node and creates links to them with probability  $p$ .



## Generalized Scale Free Model

- *Initial condition.*  $m$  nodes, no links.
- *Preferential attachment.* A node is added and linked to another with a probability proportional to the connectivity of the other node.
- *Intra-linking.* More nodes are added between nodes in the graph with a probability proportional to the product of the nodes connectivities.





# WEIGHTED COLLABORATION NETWORKS

- More authors  $\rightarrow$  weaker ties. (Assume tie strength  $\propto 1/(n-1)$ , where  $n$  is the number of authors.)
- Many papers together  $\rightarrow$  stronger ties. (Assume tie strength  $\propto N$ , the number of co-authored papers.)

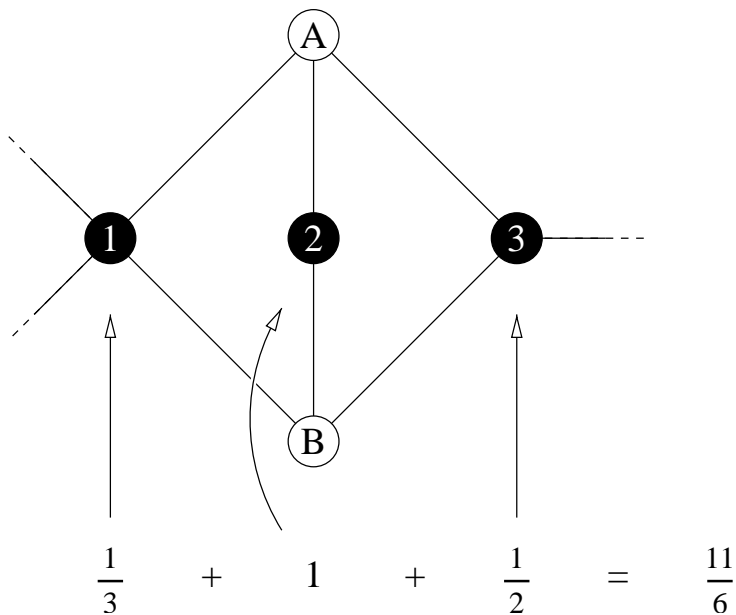
The weight,  $w_{ij}$ , of a collaboration tie:

$$w_{ij} = \sum_k \frac{\delta_i^k \delta_j^k}{n_k - 1}$$

## Weighted Betweenness

Sheer number of collaborators is no longer necessary for being well connected.

Strong connections to other highly connected collaborators also scores highly.



# HI-SCORE LISTS

	number of papers	number of co-workers	betweenness ( $\times 10^6$ )	collaboration weight
	112 Fabian, A.C.	360 Frontera, F.	2.33 Kouvelioutou, C.	16.5 Moskalenko, I.V./Strong, A.W.
	101 van Paradijs, J.	353 Kouvelioutou, C.	2.15 van Paradijs, J.	15.0 Hernquist, L./Heyl, J.S.
	81 Frontera, F.	329 van Paradijs, J.	1.80 Filippenko, A.V.	14.0 Mathews, W.G./Brighenti, F.
	80 Hernquist, L.	299 Piro, L.	1.57 Beaulieu, J.P.	13.4 Labini, F.S./Pietronero, L.
	79 Gould, A.	296 Costa, E.	1.52 Nomoto, K.	12.2 Piran, T./Sari, R.
	78 Silk, J.	291 Feroci, M.	1.52 Pian, E.	11.8 Zaldarriaga, M./Seljak, U.
	78 Klis, M.V.D.	284 Pian, E.	1.49 Frontera, F.	11.4 Hernquist, L./Katz, N.
	73 Kouvelioutou, C.	284 Hurley, K.	1.35 Silk, J.	11.1 Avila-Reese, V./Firmani, C.
	70 Ghisellini, G.	244 Palazzi, E.	1.33 Kamionkowski, M.	10.9 Dai, Z.G./Lu, T.
	66 Piro, L.	244 Heise, J.	1.28 McMahan, R.G.	10.8 Ostriker, J.P./Cen, R.
	116 Parisi, G.	107 Uchida, S.	4.11 MacDonald, A.H.	22.3 Belitz, D./Kirkpatrick, T.R.
	79 Scheffler, M.	103 Ueda, Y.	3.96 Bishop, A.R.	17.0 Shrock, R./Tsai, S.
	75 Das Sarma, S.	96 Revcolevschi, A.	3.36 Das Sarma, S.	15.0 Yukalov, V.I./Yukalova, E.P.
	74 Stanley, H.E.	94 Eisaki, H.	2.96 Tosatti, E.	14.7 Martín-Delgado, M.A./Sierra, G.
	70 MacDonald, A.H.	84 Cheong, S.	2.52 Wang, X.	14.3 Krapivsky, P.L./Ben-Naim, E.
	68 Sornette, D.	83 Isobe, M.	2.38 Revcolevschi, A.	14.1 Beenakker, C.W.J./Brouwer, P.W.
	60 Volovik, G.E.	78 Stanley, H.E.	2.30 Uchida, S.	13.8 Weng, Z.Y./Sheng, D.N.
	56 Beenakker, C.W.J.	76 Shirane, G.	2.21 Sigrist, M.	13.7 Sornette, D./Johansen, A.
	53 Dagotto, E.	76 Scheffler, M.	2.19 Cheong, S.	13.6 Rikvold, P.A./Novotny, M.A.
	50 Helbing, D.	76 Menovsky, A.A.	2.18 Stanley, H.E.	13.0 Scalapino, D.J./White, S.R.
	78 Odintsov, S.D.	50 Ambjorn, J.	0.98 Odintsov, S.D.	34.0 Lu, H./Pope, C.N.
	73 Lu, H.	44 Ferrara, S.	0.88 Ambjorn, J.	29.0 Odintsov, S.D./Nojiri, S.
	72 Pope, C.N.	43 Vafa, C.	0.88 Kogan, I.I.	18.7 Lee, H.W./Myung, Y.S.
	69 Cvetic, M.	39 Odintsov, S.D.	0.84 Henneaux, M.	18.3 Schweigert, C./Fuchs, J.
	68 Ferrara, S.	39 Kogan, I.I.	0.73 Douglas, M.R.	14.7 Ovrut, B.A./Waldram, D.
	65 Vafa, C.	36 Proeyen, A.V.	0.67 Ferrara, S.	14.7 Kleihaus, B./Kunz, J.
	65 Tseytlin, A.A.	35 Fre, P.	0.63 Vafa, C.	12.9 Mavromatos, N.E./Ellis, J.
	65 Mavromatos, N.E.	35 Ellis, J.	0.60 Khare, A.	12.4 Kachru, S./Silverstein, E.
	63 Witten, E.	35 Douglas, M.R.	0.58 Tseytlin, A.A.	11.7 Kakushadze, Z./Tye, S.H.H.
	54 Townsend, P.K.	34 Lu, H.	0.58 Townsend, P.K.	11.6 Arefeva, I.Y./Volovich, I.V.

# Hi-Score Lists

(continued)

---

rank	name	co-workers	papers
1	Rees, M. J.	31	36
2	Miralda-Escude, J.	36	34
3	Fabian, A. C.	156	112
4	Waxman, E.	15	30
5	Celotti, A.	119	45
6	Narayan, R.	65	58
7	Loeb, A.	33	64
8	Reynolds, C. S.	45	38
9	Hernquist, L.	62	80
10	Gould, A.	76	79
1	Fisher, M. P. A.	21	35
2	Balents, L.	24	29
3	MacDonald, A. H.	64	70
4	Senthil, T.	9	13
5	Das Sarma, S.	51	75
6	Millis, A. J.	43	37
7	Ioffe, L. B.	16	27
8	Sachdev, S.	28	44
9	Lee, P. A.	24	34
10	Jungwirth, T.	27	17
1	Cvetic, M.	33	69
2	Behrndt, K.	22	41
3	Tseytlin, A. A.	22	65
4	Bergshoeff, E.	21	39
5	Youm, D.	3	30
6	Lu, H.	34	73
7	Klebanov, I. R.	29	47
8	Townsend, P. K.	31	54
9	Pope, C. N.	33	72
10	Larsen, F.	11	27